

# Probing Generalized Parton Distributions through the photoproduction of a photon-meson pair

Samuel Wallon

Sorbonne Université

and

Laboratoire de Physique Théorique

CNRS / Université Paris Sud

Orsay

Diffraction - Low-x 2018

Reggio Calabria, 26 August-1 September 2018

29 August 2018

in collaboration with

B. Pire (CPHT, Palaiseau), R. Boussarie (LPT Orsay), L. Szymanowski (NCBJ, Warsaw),  
G. Duplancić, K. Passek-Kumerički (IRB, Zagreb)

based on:

JHEP 1702 (2017) 054 [arXiv:1609.03830 [hep-ph]] ( $\rho\gamma$  production)

+ paper to be submitted ( $\pi\gamma$  production)

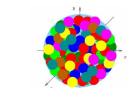
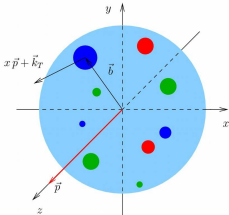
# The ultimate picture

6D/5D

Wigner distributions  
for hadrons

$$W(x, \vec{b}, k_T)$$

Experimentally  
*inaccessible* directly



3D  
perturbative Regge  
limit

uPDFs (gluons)

Unintegrated parton  
distributions

$$\int d^3 \vec{b}$$

||

TMDs

$$f(x, k_T)$$

Semi-inclusive  
processes

Transverse momentum  
dependent distributions

$$\int d^2 k_T \int d b_z$$

$$b_T \leftrightarrow \Delta$$

$$f(x, b_T)$$

Impact parameter  
distributions

$$H(x, 0, t) \longleftrightarrow H(x, \xi, t)$$

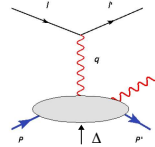
$t = -\Delta^2$

$$\int d^2 k_T \int \text{Fourier}(\vec{b})$$

$\xi=0$

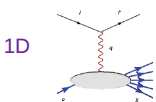
GPDs

generalised parton  
distributions



exclusive  
processes

1D

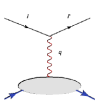
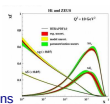


inclusive and semi-  
inclusive processes

PDFs

$$f(x)$$

parton distributions

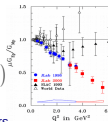


elastic processes

FFs

$$G_{E,M}(t)$$

form factors



$$\int dx x^{n-1}$$

GFFs

generalized form factors

lattices

# Extensions from DIS

- DIS: inclusive process  $\rightarrow$  forward amplitude ( $t = 0$ ) (optical theorem)

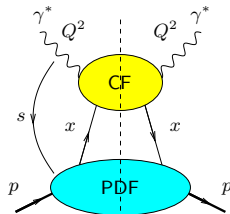
(DIS: Deep Inelastic Scattering)

ex:  $e^\pm p \rightarrow e^\pm X$  at HERA

$x \Rightarrow$  1-dimensional structure

Structure Function

$$= \text{Coefficient Function (hard)} \otimes \text{Parton Distribution Function (soft)}$$



- DVCS: exclusive process  $\rightarrow$  non forward amplitude ( $-t \ll s = W^2$ )

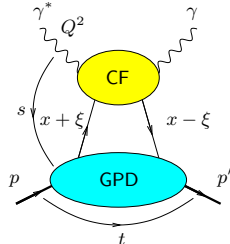
(DVCS: Deep Virtual Compton Scattering)

Fourier transf.:  $t \leftrightarrow$  impact parameter

$(x, t) \Rightarrow$  3-dimensional structure

Amplitude

$$= \text{Coefficient Function (hard)} \otimes \text{Generalized Parton Distribution (soft)}$$

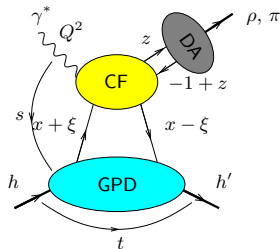


Müller et al. '91 - '94; Radyushkin '96; Ji '97

## Extensions from DVCS

- **Meson production:**  $\gamma$  replaced by  $\rho, \pi, \dots$

$$\begin{aligned}
 & \text{Amplitude} \\
 = & \quad \text{GPD (soft)} \quad \otimes \quad \text{CF (hard)} \quad \otimes \quad \text{Distribution Amplitude (soft)}
 \end{aligned}$$



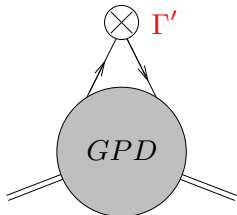
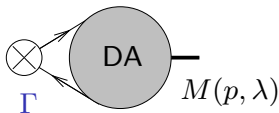
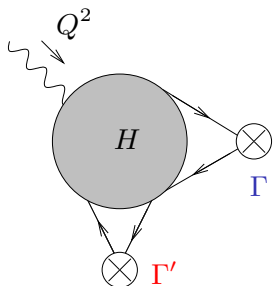
Collins, Frankfurt, Strikman '97; Radyushkin '97

proofs valid only for some restricted cases

# Collinear factorization

Meson electroproduction: factorization with a GPD and a DA

## The building blocks



$\Gamma, \Gamma'$  : Dirac matrices compatible  
with quantum numbers:  $C, P, T, \text{chirality}$

Similar structure for gluon exchange

## Collinear factorization

## Twist 2 GPDs

## Classification of twist 2 GPDs

- For quarks, one should distinguish the exchanges
  - without helicity flip (chiral-even  $\Gamma'$  matrices): 4 chiral-even GPDs:

$$H^q \xrightarrow{\xi=0, t=0} \text{PDF } q, E^q, \tilde{H}^q \xrightarrow{\xi=0, t=0} \text{polarized PDFs } \Delta q, \tilde{E}^q$$

$$\begin{aligned} F^q &= \frac{1}{2} \int \frac{dz^+}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q}(-\frac{1}{2}z) \gamma^+ q(\frac{1}{2}z) | p \rangle \Big|_{z^+=0, z_\perp=0} \\ &= \frac{1}{2P^+} \left[ H^q(x, \xi, t) \bar{u}(p') \gamma^+ u(p) + E^q(x, \xi, t) \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2m} u(p) \right], \end{aligned}$$

$$\begin{aligned} \tilde{F}^q &= \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q}(-\frac{1}{2}z) \gamma^+ \gamma_5 q(\frac{1}{2}z) | p \rangle \Big|_{z^+=0, z_\perp=0} \\ &= \frac{1}{2P^+} \left[ \tilde{H}^q(x, \xi, t) \bar{u}(p') \gamma^+ \gamma_5 u(p) + \tilde{E}^q(x, \xi, t) \bar{u}(p') \frac{\gamma_5 \Delta^+}{2m} u(p) \right]. \end{aligned}$$

- with helicity flip (chiral-odd  $\Gamma'$  mat.): 4 chiral-odd GPDs:

$$H_T^q \xrightarrow{\xi=0, t=0} \text{quark transversity PDFs } \delta q, E_T^q, \tilde{H}_T^q, \tilde{E}_T^q$$

$$\begin{aligned} &\frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q}(-\frac{1}{2}z) i\sigma^{+i} q(\frac{1}{2}z) | p \rangle \Big|_{z^+=0, z_\perp=0} \\ &= \frac{1}{2P^+} \bar{u}(p') \left[ H_T^q i\sigma^{+i} + \tilde{H}_T^q \frac{P^+ \Delta^i - \Delta^+ P^i}{m^2} + E_T^q \frac{\gamma^+ \Delta^i - \Delta^+ \gamma^i}{2m} + \tilde{E}_T^q \frac{\gamma^+ P^i - P^+ \gamma^i}{m} \right] \end{aligned}$$

# Collinear factorization

## Twist 2 GPDs

### Classification of twist 2 GPDs

- analogously, for gluons:

- 4 gluonic GPDs without helicity flip:

$$\begin{matrix} H^g \\ E^g \end{matrix} \xrightarrow{\xi=0, t=0} \text{PDF } x g$$

$$\begin{matrix} \tilde{H}^g \\ \tilde{E}^g \end{matrix} \xrightarrow{\xi=0, t=0} \text{polarized PDF } x \Delta g$$

- 4 gluonic GPDs with helicity flip:

$$\begin{matrix} H_T^g \\ E_T^g \\ \tilde{H}_T^g \\ \tilde{E}_T^g \end{matrix}$$

(no forward limit reducing to gluons PDFs here: a change of 2 units of helicity cannot be compensated by a spin 1/2 target)

# Chiral-odd sector: Transversity of the nucleon using hard processes

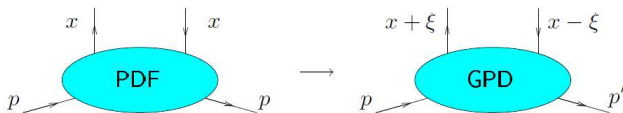
## What is transversity?

- Transverse spin content of the proton:

$$\begin{aligned}
 |\uparrow\rangle(x) &\sim |\rightarrow\rangle + |\leftarrow\rangle \\
 |\downarrow\rangle(x) &\sim |\rightarrow\rangle - |\leftarrow\rangle
 \end{aligned}$$

spin along  $x$                       helicity states

- Observables which are sensitive to helicity flip thus give access to transversity  $\Delta_T q(x)$ . Poorly known.
- Transversity GPDs are completely unknown experimentally.



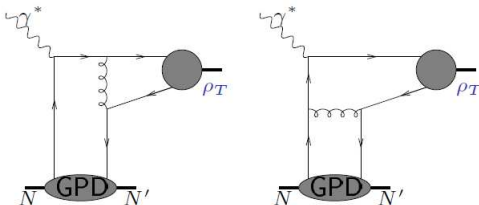
- For massless (anti)particles, chirality = (-)helicity
- Transversity is thus a chiral-odd quantity
- Since (in the massless limit) QCD and QED are chiral-even ( $\gamma^\mu, \gamma^\mu \gamma^5$ ), the chiral-odd quantities ( $1, \gamma^5, [\gamma^\mu, \gamma^\nu]$ ) which one wants to measure should appear in pairs



# Transversity of the nucleon using hard processes: using a two body final state process?

## How to get access to transversity GPDs?

- the dominant DA of  $\rho_T$  is of twist 2 and chiral-odd ( $[\gamma^\mu, \gamma^\nu]$  coupling)
- unfortunately  $\gamma^* N^\uparrow \rightarrow \rho_T N' = 0$ 
  - This cancellation is true at any order : such a process would require a helicity transfer of 2 from a photon.
  - lowest order diagrammatic argument:



$$\gamma^\alpha [\gamma^\mu, \gamma^\nu] \gamma_\alpha \rightarrow 0$$

[Diehl, Gousset, Pire], [Collins, Diehl]

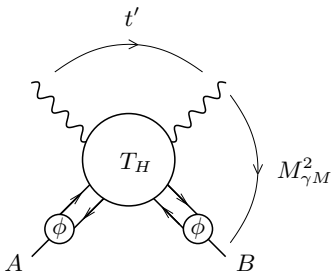
# Transversity of the nucleon using hard processes: using a two body final state process?

## Can one circumvent this vanishing?

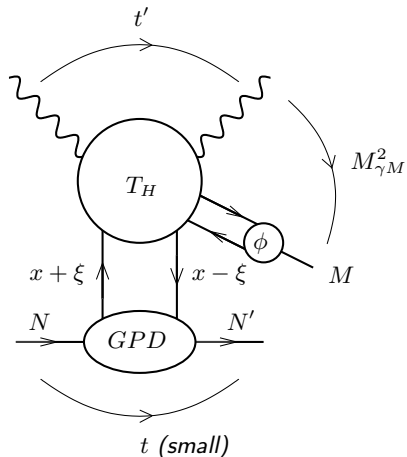
- This vanishing only occurs at **twist 2**
- At twist 3 this process does not vanish [Ahmad, Goldstein, Liuti], [Goloskokov, Kroll]
- However processes involving **twist 3 DAs** may face problems with factorization (end-point singularities)  
can be made safe in the high-energy  $k_T$ -factorization approach [Anikin, Ivanov, Pire, Szymanowski, S.W.]
- One can also consider a 3-body final state process [Ivanov, Pire, Szymanowski, Teryaev], [Enberg, Pire, Szymanowski], [El Beiyad, Pire, Segond, Szymanowski, S. W.]

# Probing GPDs using $\rho$ or $\pi$ meson + photon production

- We consider the process  $\gamma N \rightarrow \gamma M N'$   $M = \text{meson}$
- Collinear factorization of the amplitude for  $\gamma + N \rightarrow \gamma + M + N'$  at large  $M_{\gamma M}^2$

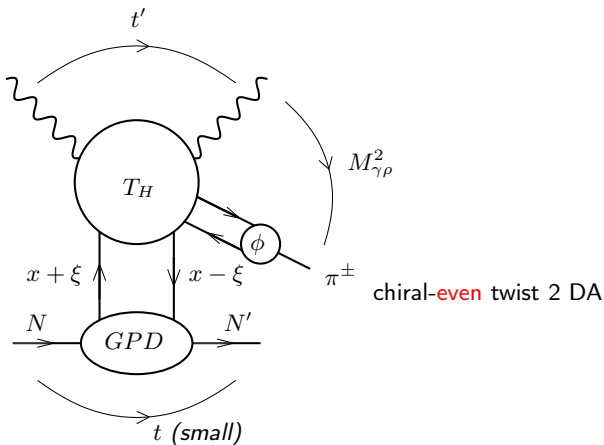


large angle factorization  
à la Brodsky Lepage



# Probing **chiral-even** GPDs using $\pi$ meson + photon production

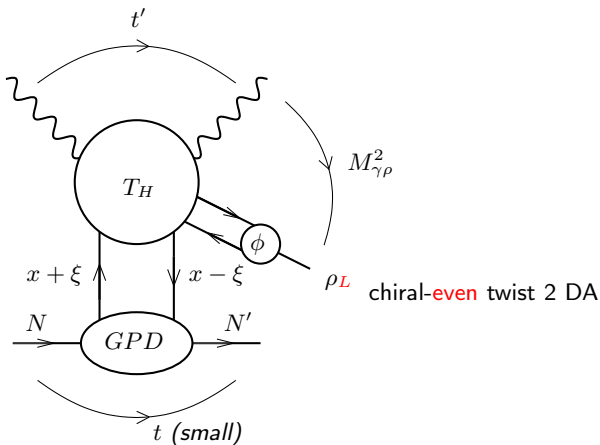
Processes with **3 body final states** can give access to **chiral-even GPDs**



**chiral-even** twist 2 GPD

# Probing **chiral-even** GPDs using $\rho$ meson + photon production

Processes with **3 body final states** can give access to **chiral-even GPDs**

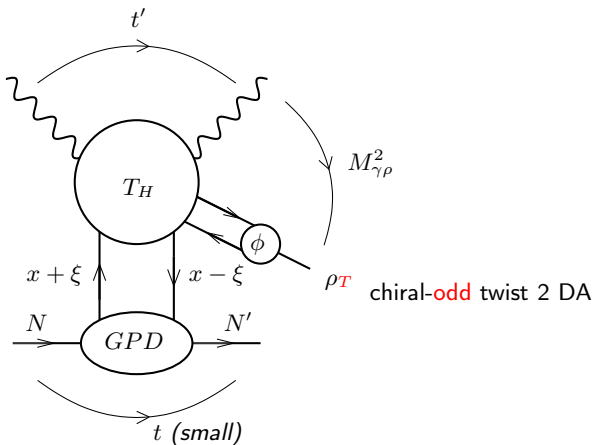


$\rho_L$  **chiral-even** twist 2 DA

**chiral-even** twist 2 GPD

# Probing **chiral-odd** GPDs using $\rho$ meson + photon production

Processes with **3 body final states** can give access to **chiral-odd GPDs**

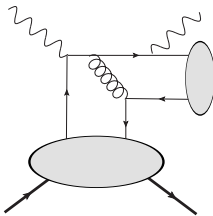


chiral-odd twist 2 GPD

# Probing **chiral-odd** GPDs using $\rho$ meson + photon production

Processes with **3 body final states** can give access to **chiral-odd GPDs**

How did we manage to circumvent the no-go theorem for  $2 \rightarrow 2$  processes?



Typical non-zero diagram for a **transverse**  $\rho$  meson

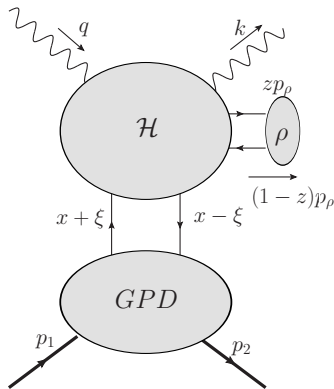
the  $\sigma$  matrices (from DA and GPD sides) do not kill it anymore!

# Master formula based on leading twist 2 factorization

## The $\rho$ example

$$\mathcal{A} \propto \int_{-1}^1 dx \int_0^1 dz T(x, \xi, z) \times H(x, \xi, t) \Phi_\rho(z) + \dots$$

- Both the DA and the GPD can be either **chiral-even** or **chiral-odd**.
- At twist 2 the **longitudinal  $\rho$  DA** is **chiral-even** and the **transverse  $\rho$  DA** is **chiral-odd**.
- Hence we will need both **chiral-even** and **chiral-odd** non-perturbative building blocks and hard parts.





## Kinematics

## Kinematics to handle GPD in a 3-body final state process

- use a **Sudakov** basis :  
light-cone vectors  $p$ ,  $n$  with  $2p \cdot n = s$
- assume the following kinematics:
  - $\Delta_{\perp} \ll p_{\perp}$
  - $M^2, m_{\rho}^2 \ll M_{\gamma\rho}^2$

- initial state particle momenta:

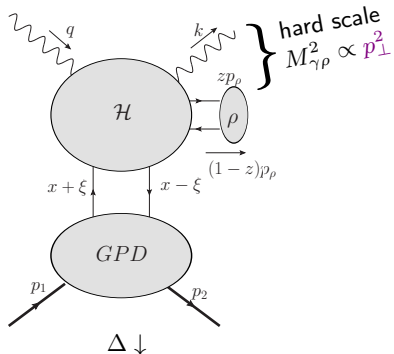
$$q^{\mu} = n^{\mu}, \quad p_1^{\mu} = (1 + \xi) p^{\mu} + \frac{M^2}{s(1+\xi)} n^{\mu}$$

- final state particle momenta:

$$p_2^{\mu} = (1 - \xi) p^{\mu} + \frac{M^2 + \vec{p}_t^2}{s(1 - \xi)} n^{\mu} + \Delta_{\perp}^{\mu}$$

$$k^{\mu} = \alpha n^{\mu} + \frac{(\vec{p}_t - \vec{\Delta}_t/2)^2}{\alpha s} p^{\mu} + p_{\perp}^{\mu} - \frac{\Delta_{\perp}^{\mu}}{2},$$

$$p_{\rho}^{\mu} = \alpha_{\rho} n^{\mu} + \frac{(\vec{p}_t + \vec{\Delta}_t/2)^2 + m_{\rho}^2}{\alpha_{\rho} s} p^{\mu} - p_{\perp}^{\mu} - \frac{\Delta_{\perp}^{\mu}}{2},$$



# Non perturbative **chiral-even** building blocks

- Helicity conserving GPDs at twist 2 :

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left( -\frac{1}{2}z^- \right) \gamma^+ \psi \left( \frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle$$

$$= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[ H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) \frac{i\sigma^{\alpha+} \Delta_\alpha}{2m} \right]$$

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left( -\frac{1}{2}z^- \right) \gamma^+ \gamma^5 \psi \left( \frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle$$

$$= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[ \tilde{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \tilde{E}^q(x, \xi, t) \frac{\gamma^5 \Delta^+}{2m} \right]$$

- We will consider the simplest case when  $\Delta_\perp = 0$ .
- In that case and in the forward limit  $\xi \rightarrow 0$  only the  $H^q$  and  $\tilde{H}^q$  terms survive.
- Helicity conserving (vector) DA at twist 2 :

$$\langle 0 | \bar{u}(0) \gamma^\mu u(x) | \rho^0(p, s) \rangle = \frac{p^\mu}{\sqrt{2}} f_\rho \int_0^1 du e^{-iup \cdot x} \phi_{\parallel}(u)$$

# Non perturbative **chiral-odd** building blocks

- Helicity flip GPD at twist 2 :

$$\begin{aligned}
 & \int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left( -\frac{1}{2}z^- \right) i\sigma^{+i} \psi \left( \frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle \\
 = & \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[ H_T^q(x, \xi, t) i\sigma^{+i} + \tilde{H}_T^q(x, \xi, t) \frac{P^+ \Delta^i - \Delta^+ P^i}{M_N^2} \right. \\
 + & \left. E_T^q(x, \xi, t) \frac{\gamma^+ \Delta^i - \Delta^+ \gamma^i}{2M_N} + \tilde{E}_T^q(x, \xi, t) \frac{\gamma^+ P^i - P^+ \gamma^i}{M_N} \right] u(p_1, \lambda_1)
 \end{aligned}$$

- We will consider the simplest case when  $\Delta_\perp = 0$ .
- In that case and in the forward limit  $\xi \rightarrow 0$  **only the  $H_T^q$  term survives.**
- Transverse  $\rho$  DA at twist 2 :

$$\langle 0 | \bar{u}(0) \sigma^{\mu\nu} u(x) | \rho^0(p, s) \rangle = \frac{i}{\sqrt{2}} (\epsilon_\rho^\mu p^\nu - \epsilon_\rho^\nu p^\mu) f_\rho^\perp \int_0^1 du e^{-iup \cdot x} \phi_\perp(u)$$

## Models for DAs

## Asymptotical DAs

- We take the simplistic asymptotic form of the (normalized) DAs (i.e. no evolution):

$$\phi_{\pi}(z) = \phi_{\rho\parallel}(z) = \phi_{\rho\perp}(z) = 6z(1-z).$$

- For the  $\pi$  case, a non asymptotical wave function can be also investigated:

$$\phi_{\pi}(z) = \frac{8}{\pi} \sqrt{z(1-z)}.$$

*(under investigation)*

# Model for GPDs: based on the Double Distribution ansatz

## Realistic Parametrization of GPDs

- GPDs can be represented in terms of **Double Distributions** [Radyushkin] based on the **Schwinger** representation of a toy model for GPDs which has the structure of a triangle diagram in scalar  $\phi^3$  theory

$$H^q(x, \xi, t = 0) = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(\beta + \xi\alpha - x) f^q(\beta, \alpha)$$

- ansatz for these Double Distributions [Radyushkin]:

- chiral-even sector:

$$f^q(\beta, \alpha, t = 0) = \Pi(\beta, \alpha) q(\beta) \Theta(\beta) - \Pi(-\beta, \alpha) \bar{q}(-\beta) \Theta(-\beta),$$

$$\tilde{f}^q(\beta, \alpha, t = 0) = \Pi(\beta, \alpha) \Delta q(\beta) \Theta(\beta) + \Pi(-\beta, \alpha) \Delta \bar{q}(-\beta) \Theta(-\beta).$$

- chiral-odd sector:

$$f_T^q(\beta, \alpha, t = 0) = \Pi(\beta, \alpha) \delta q(\beta) \Theta(\beta) - \Pi(-\beta, \alpha) \delta \bar{q}(-\beta) \Theta(-\beta),$$

- $\Pi(\beta, \alpha) = \frac{3}{4} \frac{(1-\beta)^2 - \alpha^2}{(1-\beta)^3}$  : profile function

- simplistic factorized ansatz for the  $t$ -dependence:

$$H^q(x, \xi, t) = H^q(x, \xi, t = 0) \times F_H(t)$$

with  $F_H(t) = \frac{C^2}{(t-C)^2}$  a standard **dipole form factor** ( $C = .71$  GeV)

# Model for GPDs: based on the Double Distribution ansatz

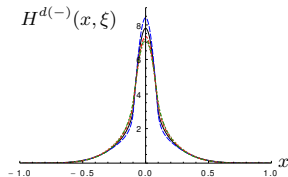
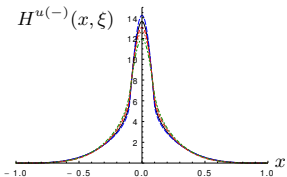
## Sets of used PDFs

- $q(x)$  : unpolarized PDF [GRV-98]  
and [MSTW2008lo, MSTW2008nnlo, ABM11nnlo, CT10nnlo]
- $\Delta q(x)$  polarized PDF [GRSV-2000]
- $\delta q(x)$  : transversity PDF [Anselmino *et al.*]

# Model for GPDs: based on the Double Distribution ansatz

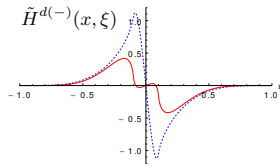
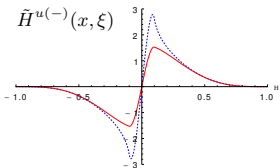
Typical sets of chiral-even GPDs ( $C = -1$  sector)

$$\xi = .1 \leftrightarrow S_{\gamma N} = 20 \text{ GeV}^2 \text{ and } M_{\gamma\rho}^2 = 3.5 \text{ GeV}^2$$



$$H^{q(-)}(x, \xi, t) = H^q(x, \xi, t) + H^q(-x, \xi, t)$$

five Ansätze for  $q(x)$ : GRV-98, MSTW2008lo, MSTW2008nnlo, ABM11nnlo, CT10nnlo



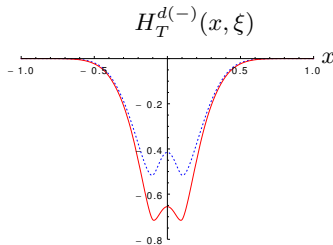
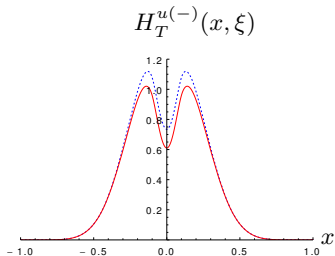
$$\tilde{H}^{q(-)}(x, \xi, t) = \tilde{H}^q(x, \xi, t) - \tilde{H}^q(-x, \xi, t)$$

“valence” and “standard”: two GRSV Ansätze for  $\Delta q(x)$

## Model for GPDs: based on the Double Distribution ansatz

Typical sets of chiral-odd GPDs ( $C = -1$  sector)

$$\xi = .1 \leftrightarrow S_{\gamma N} = 20 \text{ GeV}^2 \text{ and } M_{\gamma\rho}^2 = 3.5 \text{ GeV}^2$$



$$H_T^{q(-)}(x, \xi, t) = H_T^q(x, \xi, t) + H_T^q(-x, \xi, t)$$

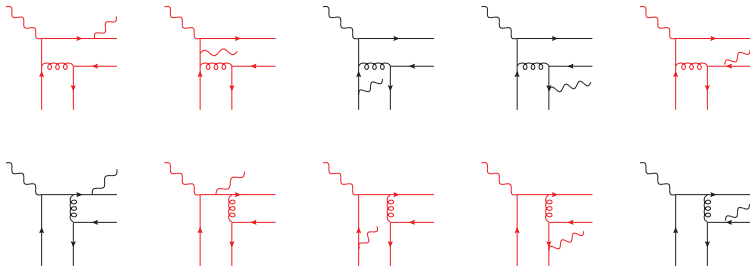
"valence" and "standard": two GRSV Ansätze for  $\Delta q(x)$

$\Rightarrow$  two Ansätze for  $\delta q(x)$



# Computation of the hard part

20 diagrams to compute



- The other half can be deduced by  $q \leftrightarrow \bar{q}$  (anti)symmetry depending on  $C$ -parity in  $t$ -channel
- Red diagrams cancel in the chiral-odd case

## Final computation

## Final computation

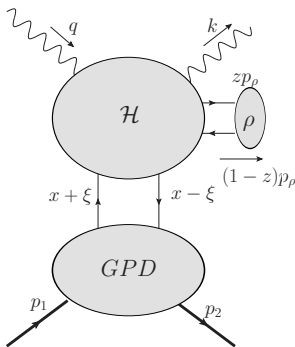
$$\mathcal{A} \propto \int_{-1}^1 dx \int_0^1 dz T(x, \xi, z) H(x, \xi, t) \Phi_\rho(z)$$

- One performs the  $z$  integration **analytically** using an asymptotic DA  $\propto z(1-z)$
- One then plugs our GPD models into the formula and performs the integral w.r.t.  $x$  numerically.
- Differential cross section:

$$\left. \frac{d\sigma}{dt du' dM_{\gamma\rho}^2} \right|_{-t=(-t)_{min}} = \frac{|\overline{\mathcal{M}}|^2}{32S_{\gamma N}^2 M_{\gamma\rho}^2 (2\pi)^3}.$$

$|\overline{\mathcal{M}}|^2 =$  averaged amplitude squared

- Kinematical parameters:  $S_{\gamma N}^2$ ,  $M_{\gamma\rho}^2$  and  $-u'$

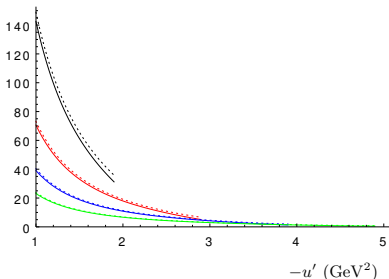


Fully differential cross section:  $\rho_L$ 

## Chiral even cross section

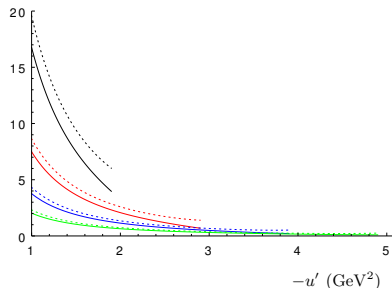
at  $-t = (-t)_{\min}$ 

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u') d(-t)} \text{ (pb} \cdot \text{GeV}^{-6}\text{)}$$



proton target

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u') d(-t)} \text{ (pb} \cdot \text{GeV}^{-6}\text{)}$$



neutron target

$$S_{\gamma N} = 20 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 3, 4, 5, 6 \text{ GeV}^2$$

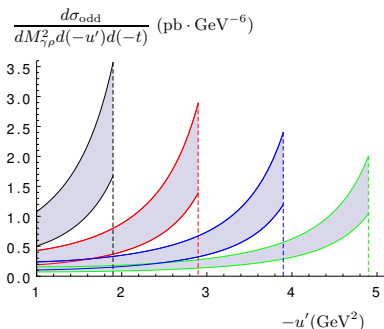
solid: "valence" model

dotted: "standard" model

# Fully differential cross section: $\rho_T$

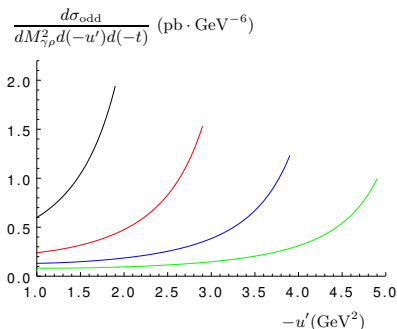
## Chiral odd cross section

at  $-t = (-t)_{\min}$



proton target

"valence" and "standard" models,  
each of them with  $\pm 2\sigma$  [S. Melis]



neutron target

"valence" model only

$$S_{\gamma N} = 20 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 3, 4, 5, 6 \text{ GeV}^2$$

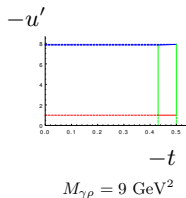
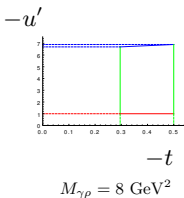
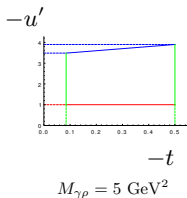
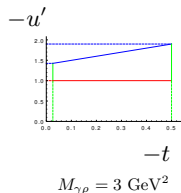
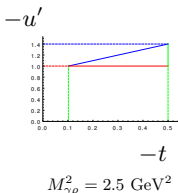
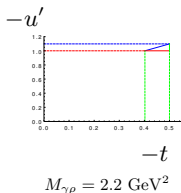
## Phase space integration

Evolution of the phase space in  $(-t, -u')$  plane

large angle scattering:  $M_{\gamma\rho}^2 \sim -u' \sim -t'$

in practice:  $-u' > 1 \text{ GeV}^2$  and  $-t' > 1 \text{ GeV}^2$  and  $(-t)_{\min} \leq -t \leq .5 \text{ GeV}^2$   
 this ensures large  $M_{\gamma\rho}^2$

example:  $S_{\gamma N} = 20 \text{ GeV}^2$



## Variation with respect to $S_{\gamma N}$

$$\text{Mapping } (S_{\gamma N}, M_{\gamma\rho}) \mapsto (\tilde{S}_{\gamma N}, \tilde{M}_{\gamma\rho})$$

One can save a lot of CPU time:

- $\mathcal{M}(\alpha, \xi)$  and  $GPDs(\xi, x)$
- In the generalized Bjorken limit:
  - $\alpha = \frac{-u'}{M_{\gamma\rho}^2}$
  - $\xi = \frac{M_{\gamma\rho}^2}{2(S_{\gamma N} - M^2) - M_{\gamma\rho}^2}$

Given  $S_{\gamma N}$  ( $= 20 \text{ GeV}^2$ ), with its grid in  $M_{\gamma\rho}^2$ , choose another  $\tilde{S}_{\gamma N}$ .

One can get the corresponding grid in  $\tilde{M}_{\gamma\rho}$  by just keeping the same  $\xi$ 's:

$$\tilde{M}_{\gamma\rho}^2 = M_{\gamma\rho}^2 \frac{\tilde{S}_{\gamma N} - M^2}{S_{\gamma N} - M^2},$$

From the grid in  $-u'$ , the new grid in  $-\tilde{u}'$  is given by just keeping the same  $\alpha$ 's:

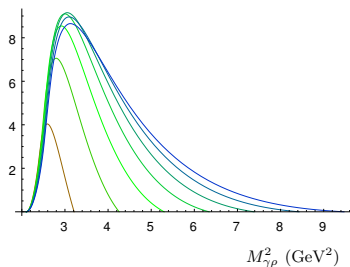
$$-\tilde{u}' = \frac{\tilde{M}_{\gamma\rho}^2}{M_{\gamma\rho}^2} (-u').$$

$\Rightarrow$  a single set of numerical computations is required (we take  $S_{\gamma N} = 20 \text{ GeV}^2$ )

# Single differential cross section: $\rho_L$

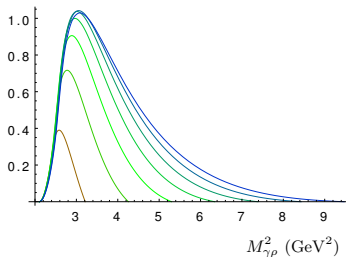
## Chiral even cross section

$$\frac{d\sigma_{even}}{dM_{\gamma\rho}^2} \text{ (pb} \cdot \text{GeV}^{-2}\text{)}$$



proton target

$$\frac{d\sigma_{even}}{dM_{\gamma\rho}^2} \text{ (pb} \cdot \text{GeV}^{-2}\text{)}$$



neutron target

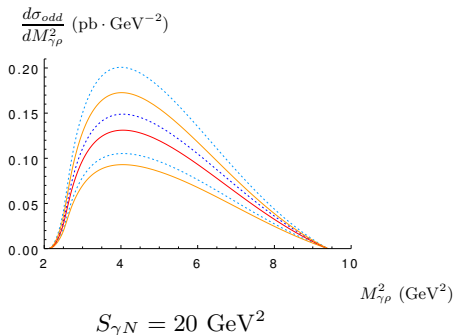
"valence" scenario

$S_{\gamma N}$  vary in the set 8, 10, 12, 14, 16, 18, 20 GeV<sup>2</sup> (from left to right)

typical JLab kinematics

Single differential cross section:  $\rho_T$ 

## Chiral odd cross section



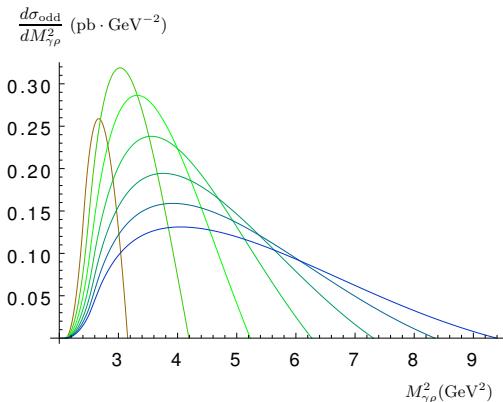
Various ansätze for the PDFs  $\Delta q$  used to build the GPD  $H_T$ :

- *dotted curves*: “standard” scenario
- *solid curves*: “valence” scenario
- *deep-blue* and *red* curves: central values
- *light-blue* and *orange*: results with  $\pm 2\sigma$ .



# Single differential cross section: $\rho_T$

## Chiral odd cross section



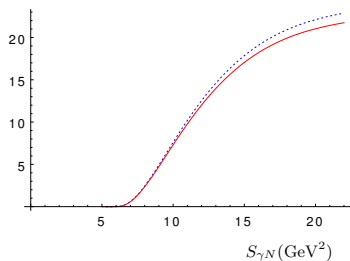
proton target, "valence" scenario

$S_{\gamma N}$  vary in the set 8, 10, 12, 14, 16, 18, 20 GeV<sup>2</sup> (from left to right)

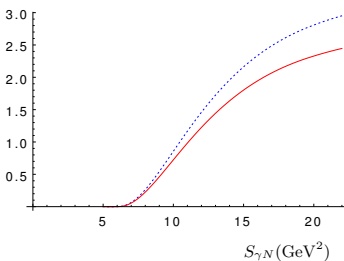
typical JLab kinematics

Integrated cross-section:  $\rho_L$ 

## Chiral even cross section

 $\sigma_{even}$  (pb)

proton target

 $\sigma_{even}$  (pb)

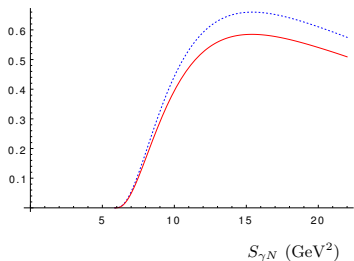
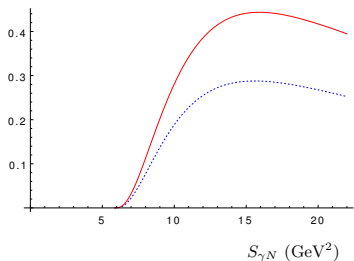
neutron target

solid red: "valence" scenario

dashed blue: "standard" one

Integrated cross-section:  $\rho_T$ 

## Chiral odd cross section

 $\sigma_{odd}$  (pb) $\sigma_{odd}$  (pb)

solid red: "valence" scenario

dashed blue: "standard" one

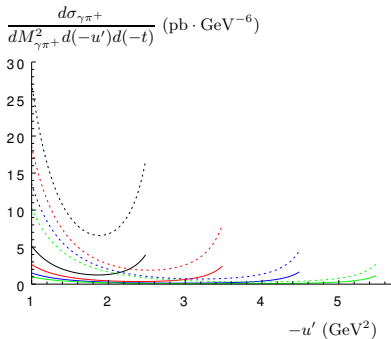
## Counting rates for 100 days: $\rho$

example: JLab Hall B

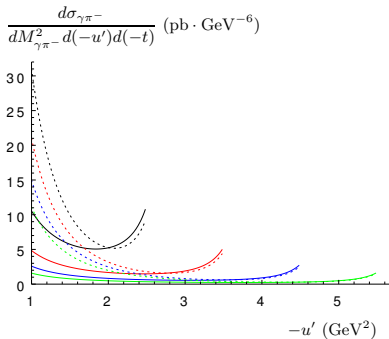
- untagged incoming  $\gamma \Rightarrow$  Weizsäcker-Williams distribution
- With an expected luminosity of  $\mathcal{L} = 100 \text{ nb}^{-1} \text{ s}^{-1}$ , for 100 days of run:
  - Chiral even case :  $\simeq 1.9 \cdot 10^5 \rho_L$ .
  - Chiral odd case :  $\simeq 7.5 \cdot 10^3 \rho_T$

# Fully differential cross section: $\pi^\pm$ PRELIMINARY

Chiral even sector:  $\pi^\pm$   
 at  $-t = (-t)_{\min}$



$\pi^+$  photoproduction (proton target)



$\pi^-$  photoproduction (neutron target)

$$S_{\gamma N} = 20 \text{ GeV}^2$$

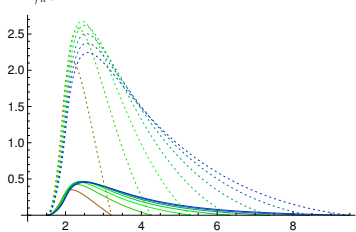
$$M_{\gamma\rho}^2 = 3, 4, 5, 6 \text{ GeV}^2$$

solid: "valence" model  
 dotted: "standard" model

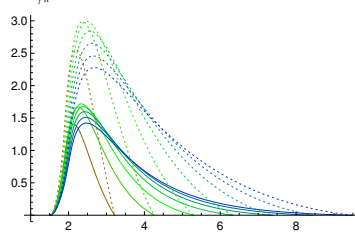
Single differential cross section:  $\pi^\pm$  PRELIMINARY

Chiral even sector:  $\pi^\pm$

$$\frac{d\sigma_{\gamma\pi^+}}{dM^2_{\gamma\pi^+}} \text{ (pb} \cdot \text{GeV}^{-2}\text{)}$$



$$\frac{d\sigma_{\gamma\pi^-}}{dM^2_{\gamma\pi^-}} \text{ (pb} \cdot \text{GeV}^{-2}\text{)}$$

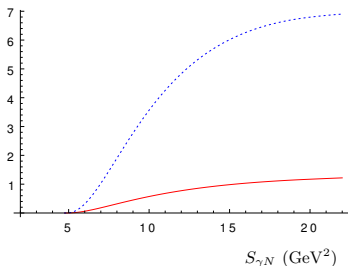
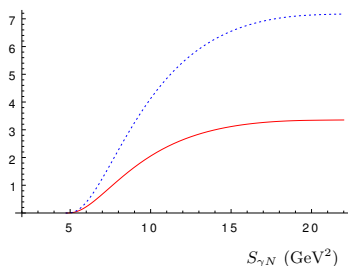


$\pi^+$  photoproduction (proton target)

$\pi^-$  photoproduction (neutron target)

$S_{\gamma N}$  vary in the set 8, 10, 12, 14, 16, 18, 20 GeV<sup>2</sup> (from left to right)

solid: "valence" model  
dotted: "standard" model

Chiral even sector:  $\pi^\pm$  $\sigma_{\gamma\pi^+}$  (pb) $\sigma_{\gamma\pi^-}$  (pb) $\pi^+$  photoproduction (proton target)     $\pi^-$  photoproduction (neutron target)

solid red: "valence" scenario

dashed blue: "standard" one

Counting rates for 100 days:  $\pi^\pm$ 

example: JLab Hall B

- untagged incoming  $\gamma \Rightarrow$  Weizsäcker-Williams distribution
- With an expected luminosity of  $\mathcal{L} = 100 \text{ nb}^{-1} \text{ s}^{-1}$ , for 100 days of run:
  - $\pi^+$  :  $\simeq 10^4$
  - $\pi^-$  :  $\simeq 4 \times 10^4$

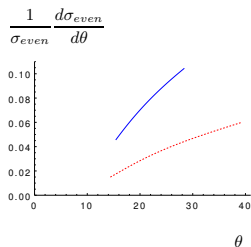


## Conclusion

- **High statistics for the chiral-even components:** enough to extract  $H$  ( $\tilde{H}$ ?) and **test the universality of GPDs** in  $\rho^0$ ,  $\rho^\pm$  (not shown) and  $\pi^\pm$  channels
- In this chiral-even sector: analogy with **Timelike Compton Scattering**, the  $\gamma\rho$  or  $\gamma\pi$  pair playing the role of the  $\gamma^*$ .
- $\rho$ -channel: chiral-even component w.r.t. the chiral-odd one:
  - $\sigma_{\text{odd}}/\sigma_{\text{even}} \sim 1/25$ .
  - possible separation  $\rho_L/\rho_T$  through an angular analysis of its decay products
  - Future: **study of polarization observables**  $\Rightarrow$  sensitive to the interference of these two amplitudes: **very sizable effect expected, of the order of 20%**
- The **Bethe Heitler** component (outgoing  $\gamma$  emitted from the incoming lepton) is:
  - zero for the chiral-odd case
  - suppressed for the chiral-even case
- Our result can also be applied to **electroproduction** ( $Q^2 \neq 0$ ) after adding **Bethe-Heitler** contributions and interferences.
- Possible measurement at **JLab** (Hall B, C, D)
- A similar study could be performed at **COMPASS**. **EIC**, **LHC** in UPC?
- **Future:**
  - Loop corrections: in progress
  - The processes  $\gamma N \rightarrow \gamma\pi^0 N'$  and  $\gamma N \rightarrow \gamma\eta^0 N'$  are of particular interest: they give an access to the gluonic GPDs at **Born** order.

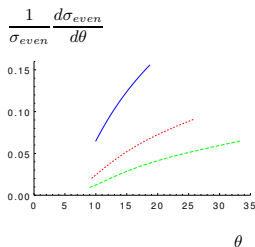
Effects of an experimental angular restriction for the produced  $\gamma$ Angular distribution of the produced  $\gamma$   
 $\rho_L$  photoproduction

after boosting to the lab frame



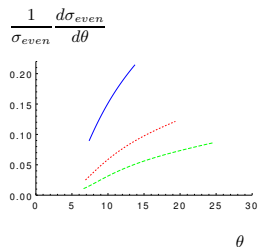
$$S_{\gamma N} = 10 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 3, 4 \text{ GeV}^2$$



$$S_{\gamma N} = 15 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 3, 4, 5 \text{ GeV}^2$$



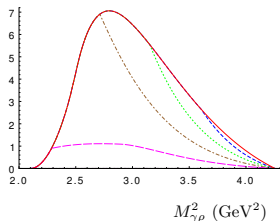
$$S_{\gamma N} = 20 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 3, 4, 5 \text{ GeV}^2$$

JLab Hall B detector equipped between  $5^\circ$  and  $35^\circ$  $\Rightarrow$  this is safe!

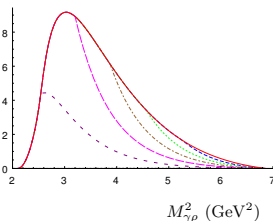
Effects of an experimental angular restriction for the produced  $\gamma$ Angular distribution of the produced  $\gamma$   
 $\rho_L$  photoproduction

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2} \text{ (pb} \cdot \text{GeV}^{-2}\text{)}$$



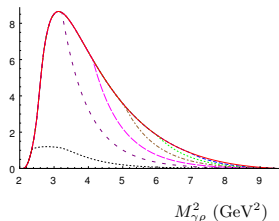
$$S_{\gamma N} = 10 \text{ GeV}^2$$

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2} \text{ (pb} \cdot \text{GeV}^{-2}\text{)}$$



$$S_{\gamma N} = 15 \text{ GeV}^2$$

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2} \text{ (pb} \cdot \text{GeV}^{-2}\text{)}$$



$$S_{\gamma N} = 20 \text{ GeV}^2$$

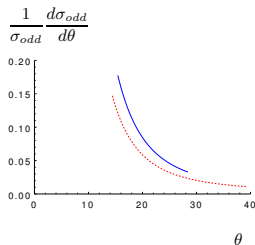
$$\theta_{\text{max}} = 35^\circ, 30^\circ, 25^\circ, 20^\circ, 15^\circ, 10^\circ$$

JLab Hall B detector equipped between  $5^\circ$  and  $35^\circ$

$\Rightarrow$  this is safe!

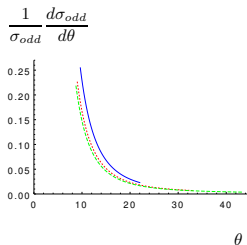
Effects of an experimental angular restriction for the produced  $\gamma$ Angular distribution of the produced  $\gamma$   
 $\rho_T$  photoproduction

after boosting to the lab frame



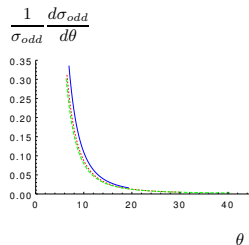
$$S_{\gamma N} = 10 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 3, 4 \text{ GeV}^2$$



$$S_{\gamma N} = 15 \text{ GeV}^2$$

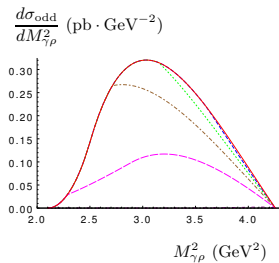
$$M_{\gamma\rho}^2 = 3.5, 5, 6.5 \text{ GeV}^2$$



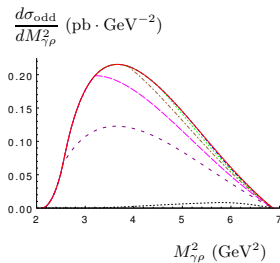
$$S_{\gamma N} = 20 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 4, 6, 8 \text{ GeV}^2$$

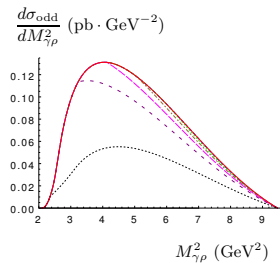
JLab Hall B detector equipped between  $5^\circ$  and  $35^\circ$  $\Rightarrow$  this is safe!

Effects of an experimental angular restriction for the produced  $\gamma$ Angular distribution of the produced  $\gamma$   
 $\rho_T$  photoproduction

$$S_{\gamma N} = 10 \text{ GeV}^2$$



$$S_{\gamma N} = 15 \text{ GeV}^2$$



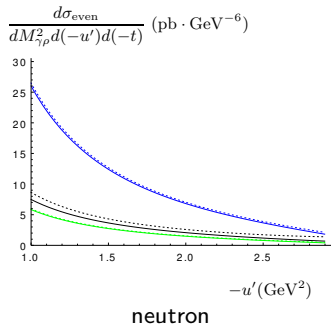
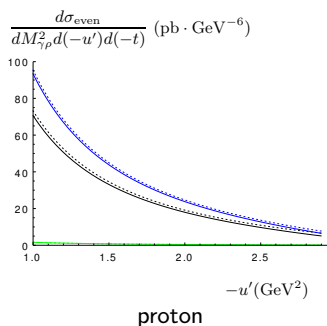
$$S_{\gamma N} = 20 \text{ GeV}^2$$

$$\theta_{\text{max}} = 35^\circ, 30^\circ, 25^\circ, 20^\circ, 15^\circ, 10^\circ$$

JLab Hall B detector equipped between 5° and 35°

⇒ this is safe!

## Chiral-even cross section

Contribution of  $u$  versus  $d$   
 $\rho_L$  photoproduction

$M_{\gamma\rho}^2 = 4 \text{ GeV}^2$ . Both vector and axial GPDs are included.

$u + d$  quarks     $u$  quark     $d$  quark

Solid: "valence" model

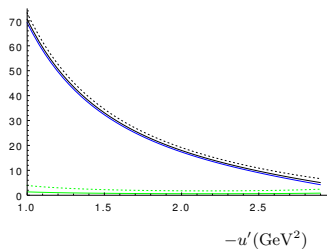
dotted: "standard" model

- $u$ -quark contribution dominates due to the charge effect

## Chiral-even cross section

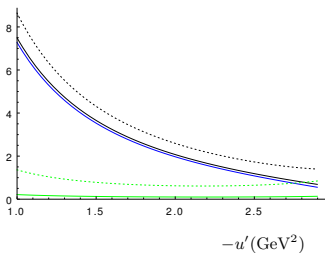
Contribution of vector versus axial amplitudes  
 $\rho_L$  photoproduction

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u')d(-t)} \quad (\text{pb} \cdot \text{GeV}^{-6})$$



proton

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u')d(-t)} \quad (\text{pb} \cdot \text{GeV}^{-6})$$



neutron

$M_{\gamma\rho}^2 = 4 \text{ GeV}^2$ . Both  $u$  and  $d$  quark contributions are included.

vector + axial amplitudes / vector amplitude / axial amplitude

solid: "valence" model

dotted: "standard" model

- dominance of the vector GPD contributions